

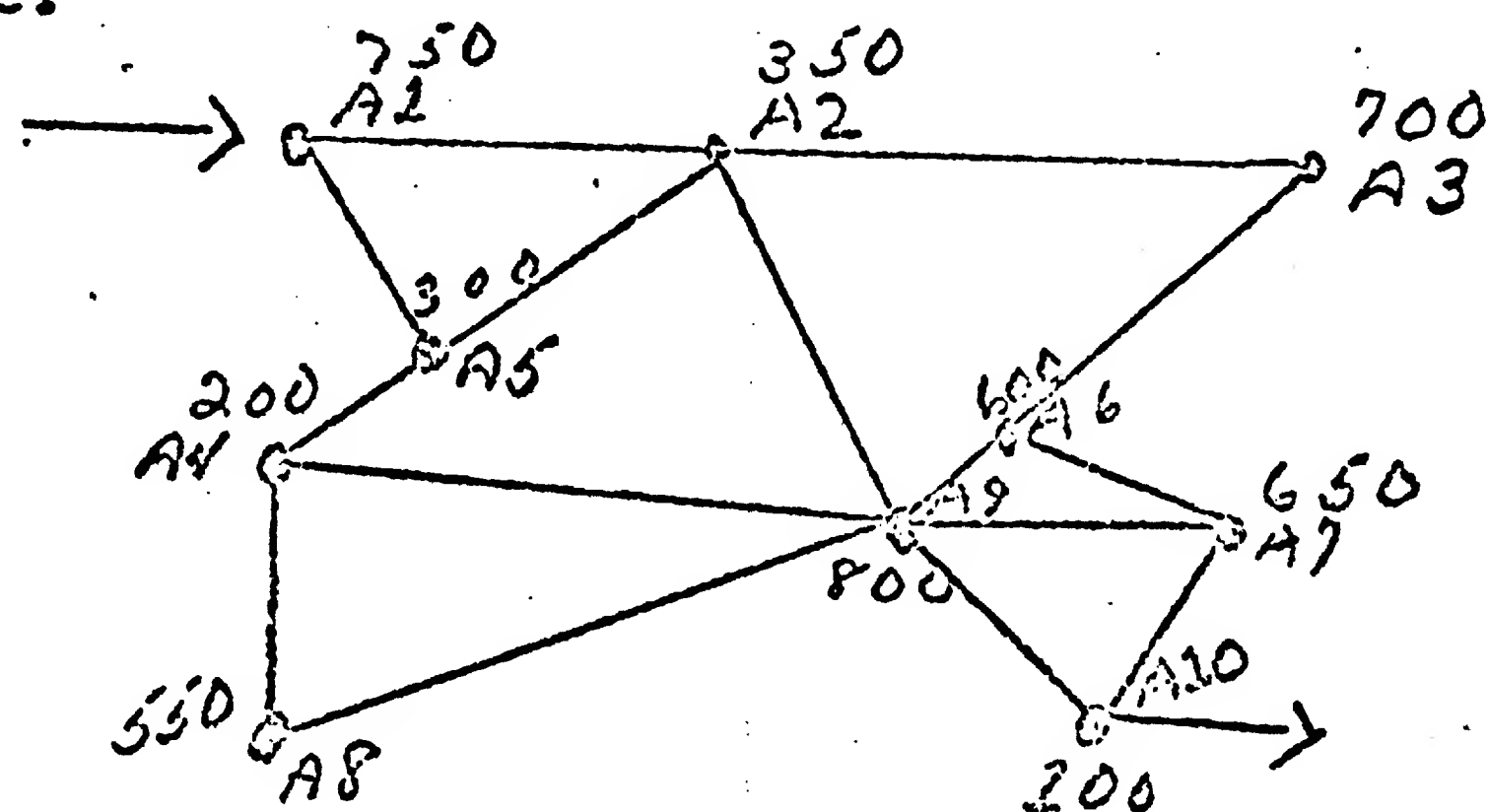
Artificial Intelligence Project--RLE and MIT Computation Center
Memo 20--Puzzle Solving Program in LISP

by
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In this note we give as an example of LISP programming a function for solving a class of puzzles in a recent prize contest.

A linear graph is given with a starting point and an endpoint. Associated with each vertex of the graph is a numerical value. The object is to find a path on the graph from the starting point to the endpoint which goes through no vertex twice and which maximizes the sum of the values associated with the vertices through which the path goes.

Example:



We shall use the following conventions in our LISP program for solving the problem:

1. The graph is described by assigning to each vertex an atomic symbol and giving a list of terms one for each vertex, each of which is a list of three items: the name of the vertex, a list of the vertices immediately accessible from it, and the value assigned to the vertex. The graph in the example is described by:
 $((A1, (A2, A5), 7.5), (A2, (A1, A5, A9, A3), 3.5), (A3, (A2, A6), 7.0), (A4, (A5, A9, A8), 2.0), (A5, (A1, A4, A2), 3.0), (A6, (A3, A9, A7), 6.0), (A7, (A6, A9, A10), 6.5), (A8, (A4, A9), 5.5), (A9, (A3, A4, A2, A5, A7, A10), 8.0), (A10, (A7, A9), 2.0))$

2. A position is described by list of the vertices covered up to that point in reverse order. The initial position is {A1} in the example on the previous page.

3. The list of squares to which it is legal to move in a position p is given by

$$\text{legals}[p] = \text{less} [\text{car}][\text{ass2}[\text{car}[p]; p1]]; p]$$

where

$$\begin{aligned} \text{less}[m;n] &= [\text{null}[m] \rightarrow \text{NIL}; \text{occur}[\text{car}[m]; n] \rightarrow \\ &\text{less}[\text{cdr}[m]; n]; T \rightarrow \text{cons}[\text{car}[m]; \text{less}[\text{cdr}[m]; n]]] \end{aligned}$$

and

$$\begin{aligned} \text{ass2}[x;m] &= [\text{eq}[\text{caar}[m]; x] \rightarrow \text{cadr}[m]; T \rightarrow \\ &\text{ass2}[x; \text{cdr}[m]]] \end{aligned}$$

and

$$\text{occur}[x;n] = \sim \text{null}[n] \wedge [\text{eq}[x; \text{car}[n]] \vee \text{occur}[x; \text{cdr}[n]]]$$

Here $\text{less}[m;n]$ is a list of those elements of m not members of n . $\text{ass2}[x;m]$ is cdr [the first element of m , car of which is x]. $\text{occur}[x;m]$ is the predicate that asserts that x is a member of m .

4. The best path is given by $\text{best}[\text{initial position}; \text{moves from the initial position; path with very low value}]$ or in the present example, $\text{best}[(A1); (A2, A5); (A1)]$. The function $\text{best}[p;m;s]$ is the best path starting with the subpath p , where the moves from p are to be taken from the list m and s is the best path found so far. We have

$$\begin{aligned} \text{best}[p;m;s] &= [\text{null}[m] \rightarrow s; T \rightarrow \text{best}[p; \text{cch}[m]; \text{MINUS}[\text{eq}[\text{car}[n]; \\ &H] \rightarrow \text{better}[p;s] \rightarrow p; T \rightarrow s]; T \rightarrow \text{best}[n; \text{legals}[n]; s]] [\text{cons}[\text{car}[m]; \\ &p]]] \end{aligned}$$

For comparing two paths we have

$$\begin{aligned} \text{better}[p1;p2] &= \text{eq}[\text{MINUS}; \text{car}[\text{sum}[\text{addup}[p2]; \\ &\text{list}[\text{MINUS}; \text{addup}[p1]]]]] \end{aligned}$$

where

$$\text{addup}[p] = [\text{null}[p] \rightarrow 0.0; T \rightarrow \text{sum}[\text{value}[\text{car}[p]]; \text{addup}[\text{cdr}[p]]]]$$

and

$$\text{value}[sq] = \text{cadr}[\text{ass2}[sq; p1]]$$

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